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Experimental study of the turbulence intensity effects on marine current turbines behaviour. Part I: One single turbine

Paul Mycek, Benoît Gaurier, Grégory Germain, Grégory Pinon, Elie Rivoalen

Abstract

The ambient turbulence intensity in the upstream flow plays a decisive role in the behaviour of horizontal axis marine current turbines. Experimental trials, run in the IFREMER flume tank in Boulogne-Sur-Mer (France) for two different turbulence intensity rates, namely 3% and 15%, are presented. They show, for the studied turbine configuration, that while the wake of the turbine is deeply influenced by the ambient turbulence conditions, its mean performances turn out to be slightly modified. The presented conclusions are crucial in the view of implanting second generation turbines arrays. In addition, complete and detailed data sets (wake profiles and performance graphs) are made available to the scientific community in order to encourage further comparisons.

1. Introduction

The ambient turbulence intensity in the upstream flow plays a decisive role in the behaviour of horizontal axis marine current turbines. First, turbulence intensity may influence the turbine performances but, probably most important, it deeply influences the wake shape. This last issue is of crucial matter for the onset of marine current turbine arrays. Indeed, in second generation arrays, the wake of an upstream turbine may irreparably affect the power performances of another turbine positioned downstream. This aspect of elementary interactions between marine current turbines in an array will be treated in the second part of this study [1]. The present paper aims at characterising precisely the performances and wake of a single turbine depending on the ambient turbulence intensity of the incoming flow. The results of this first part will represent a strong basis for comparisons with the twin turbines setups investigated in the second part.

Several in situ studies were carried out to characterise the turbulence intensity in potential sites, where marine current turbines are expected to be installed. These studies are extremely difficult to undertake owing to their important cost, the possible harsh metocean conditions encountered, as well as the high quality measurement devices that are required to assess the turbulence intensity. Most of the studies focused on a streamwise turbulence intensity $I_x = \sigma_u/U_x$. In order to obtain a 3D turbulence intensity rate $I_x$, Milne et al. [2] precisely measured the anisotropic ratio $(\sigma_u:\sigma_v:\sigma_w) = (1:0.75:0.56)$ in the Sound of Islay (Scotland, UK); and found it similar to the values given by Nezu et Nakagawa [3]. Table 1 summarises the in situ flow measurements mentioned in the sequel. In order to obtain 3D $I_x$ values from the $I_x^{1D}$ given in all other studies, the precise $(\sigma_u:\sigma_v:\sigma_w) = (1:0.75:0.56)$ anisotropic ratio from [2] was assumed.

Among the last studies, Osalusi et al. [4,5] used an Acoustic Doppler Current Profiler (ADCP) to assess several turbulence characteristics such as Turbulent Kinetic Energy production and dissipation, Reynolds shear stresses, etc. Their study was carried out in the Fall of Warness (Orkney Islands, Scotland, UK) during a week, precisely at the tidal test site of the European Marine Energy Centre (EMEC). Following the previous assumption, the 3D turbulence intensity lies between $I_x = 7.9$–8.7% at 5 m from the seabed for a mean velocity of 1.5 m s$^{-1}$. In their in situ study, Milne et al. found a 3D turbulence intensity $I_x$ of approximately 9.5–10.3%, depending on flood and ebb tides. The measurements [2] were performed in the Sound of Islay (Scotland, UK) at 5 m from the seabed for a mean velocity of 2.0 m s$^{-1}$. They lasted approximately
15 days and used a 4 Hz ADV (Acoustic Doppler Velocimeter). Thomson et al. [6] carried out a similar study comparing two techniques respectively gave a streamwise turbulent intensity of $I_{1D} = 8.4\%$ and $I_{1D} = 11.4\%$ at the same point (the Nodule Point, Puget Sound), even with Doppler noise correction for the ADCP measurements. It should be mentioned that although ADCPs are commonly used to evaluate turbulence, potential errors can be made, essentially due to the compromise made between accuracy and resolution. Errors may also issue from the hypothesis made on the steadiness and horizontal uniformity of the turbulence, which are in contradiction with the highly intermittent and multi-scale feature of the phenomenon [9,10].

The streamwise turbulence intensities from the three previous studies [2,4 – 6] are very similar in order of magnitude, ranging from approximately 8.4% to 13%. However, the turbulence intensity $I_\sigma$ does not seem to be a global constant, or even a geographical site constant. As a matter of fact, in a recent paper, Mac Enri et al. [7] indicate that the 3D turbulence intensity $I_{1D}$ may vary from approximately 3.2% to 7.1% depending on the mean velocity, ebb and flood or neap and spring tides. At a given point, the turbulence intensity may vary significantly depending on time varying tidal physical values. Their measurements were carried out in the Strangford Narrows (Republic of Ireland), where the 1.2 MW SeaGen marine current turbine is installed. The measurements were performed at the hub level, i.e. 14 m from the seabed, with an electromagnetic current meter (Valeport Model 803) with a 1 Hz frequency. Their velocity measurements were also calibrated with an ADCP.

Spatial variations may also occur in a given geographical site. The study by Gooch et al. [11] gave varying turbulent intensity rates depending on the precise location in the Puget Sound. In fact, five locations in the Puget Sound were assessed: Admiralty Inlet, North East off the Marrowstone Lighthouse and three locations East the Marrowstone Island at the smallest cross-sectional area of the Puget Sound. The measurements, from one to two months (between 33 and 75 days), were obtained with ADCP. Small variations between ebb and flood tides were observed. However, the streamwise turbulent intensities obtained were ranging from $I_{1D} \approx 2.8$ to about 5.4% at several locations and several depths within the Puget Sound. Taking the latest results by Thomson et al. [6] into account, for a single geographical site, the streamwise turbulence intensity ratio $I_{1D}$ range lies between about 2.8% and 11.8% at different locations and different depths. Even if the turbulence intensity increases with the depth [6], these variations are however important within a single geographical site. Finally, the study by Li et al. [8] in the East River (New York, NY) gave an estimated $I_\sigma = 16\text{–}24\%$ provided that the $(\sigma_u^2, \sigma_v^2, \sigma_w^2)$ assumed ratio is still valid in the case of a river. Still, their measurements of streamwise turbulence intensity ratio $I_{1D} = 20\text{–}30\%$ are noticeably higher than the previous ones from Table 1.

The flume tank experiments presented in this paper were carried out in incoming flows with two precise turbulence intensity rates, namely $I_\sigma = 3\%$ and $I_\sigma = 15\%$. These two values are actually representative of the $I_\sigma$ range depicted in Table 1, with the minimum values of $I_\sigma \approx 3.2\%$ in the Strangford Narrows [7] to the higher values of Li et al. [8] in the East River ($I_\sigma \geq 15\%$). For the given turbine geometry used in this study, the present paper aims at describing major differences in the performances and wake characteristics between $I_\sigma = 3\%$ and 15%.

Experimental trials on a single marine current turbine in a flume tank have already been carried out, using different techniques. Bahaj et al. [12,13] carried out a power ($C_D$) and thrust ($C_T$) coefficient study on a 0.8 m-diameter turbine model in a towing tank and in a cavitation tunnel. However, in the previous two studies, the wake behind the turbine was not characterised. On the other hand, experimental wake characterisation is available in Refs. [14,15] under an actuator disc approximation. Unfortunately, this approximation does not take intrinsically into account the fluid rotation in the wake, and the power and thrust assessment is more complex. Rose et al. [16] performed several experimental trials, some in a flume tank and others in open water (Montgomery Lough) using either PIV (Particle Image Velocimetry) or ADV (Acoustic Doppler Velocimeter) techniques. Several turbines were tested, the biggest one being a 1/10th scale turbine model of 1.5 m in diameter in the lake (Montgomery Lough). However, only wake velocity measurements are presented in the paper without any turbine performance. Stallard et al. [17] also give interesting information on a single turbine wake, including turbulence intensity, even if their study mainly deals with turbine interactions. For Tedds et al. [18], many turbine performance curves are depicted depending on the number of blades, pitch angles, etc. but without much details about the wake velocity profiles. In another study, Milne et al. [19] gave interesting turbine performance and thrust curves even though their study was mainly oriented towards blade loads owing to oscillatory flows, similarly to Davies et al. [20].

The present study aims at characterising both the power and thrust coefficient curves ($C_D$ and $C_T$ curves) together with detailed wake profiles including turbulence intensities. This paper follows the same experimental procedures as presented in Ref. [21], but with an open-modified version of the turbine which enables the diffusion of the blades geometry. Some of the experimental results were partially presented or used as a matter of numerical-experimental validation in Refs. [22,23]. The present document presents all our latest experimental results of a single 3-bladed turbine immersed in two different turbulence intensities, namely $I_\sigma = 3\%$ and $I_\sigma = 15\%$.

First of all, Section 2 details the experimental setup, measurement techniques and turbine geometry. Section 3 presents the power and thrust coefficient curves, for different incoming mean velocities and the two turbulence intensity rates. The standard deviations of these curves are also shown. Then, Section 4 gives streamwise velocity, turbulence intensity and Reynolds shear stress maps depending on the two turbulence intensity rates. The wake is also characterised using integrated quantities. Finally, most of the raw results are made available in the appendices as a matter of validation with future numerical studies. This intends to answer to a recurrent request, the latest being by Churchfield et al. [24].

### 2. Experiments description

This section aims at giving a detailed description of the experimental setup and measurement facilities used for the experiments.
The definitions of the quantities that will be used for the analysis are also presented in this section.

2.1. Flume tank and experiment description

The trials were run in the IFREMER (French Research Institute for Exploitation of the Sea) wave and current flume tank, depicted in Fig. 1. The flume tank working section is 18 m long by 4 m large and 2 m deep. The streamwise flow velocity range is 0.1 to 2.2 \text{ m s}^{-1}. More details about the flume tank can be found in Ref. [25].

The experimental setup is illustrated in Fig. 2, where Cartesian coordinate system is considered, with the rotor centre as its origin \(O(0,0,0)\) and \(e_x, e_y, e_z\) as unit vectors. The flow velocity field is denoted by \(u\) and is function of the position \(x\) and time \(t\) at which it is measured. The position and velocity components are respectively denoted by \(x, y, z\), and \(u, v, w\):

\[
x = xe_x + ye_y + ze_z = (x, y, z)
\]

\[
u = ue_x + ve_y + we_z = (u, v, w)
\]  

For convenience, those components may as well be referred to in their indicial notation as \(x_i, u_i\) and \(t\) respectively, with \(i\) from 1 to 3.

2.2. Reynolds decomposition

The flow velocity field is broken down thanks to Reynolds decomposition:

\[
u(x, t) = \overline{u}(x) + u'(x, t),
\]

where \(\overline{u}\) is the time average of \(u\), defined by:

\[
\overline{u}(x) = \frac{1}{T} \int_0^T u(x, t) \, dt,
\]

where \([0; T]\) is the averaging period. Thus, \(\overline{u}\) represents the steady part of the velocity, while \(u'\) represents its fluctuating part. The components \(R_{ij}\) of the Reynolds stress tensor \(R\) are defined as follows:

\[
R_{ij} = \overline{u_i' u_j'} = (u_i - \overline{u_i})(u_j - \overline{u_j}) \quad i, j = 1, \ldots, 3.
\]  

The diagonal elements \(R_{ii}\) are denoted by \(\sigma^2(u), \sigma^2(v)\) and \(\sigma^2(w)\) in analogy with the variance in statistics.

2.3. Upstream flow conditions

The upstream turbulence intensity rate \(I_u\) is defined by:

\[
I_u = 100 \sqrt{\frac{\overline{u^2} + \overline{v^2} + \overline{w^2}}{\overline{u^2} + \overline{v^2} + \overline{w^2}}} \]

where the velocity components \(u_u, v_u, w_u\) are those of the upstream velocity \(u_u\). The LDV measurements presented in the sequel are performed in the \(xOy\) plane, the 2D upstream turbulence intensity rate is thus defined as follows:

\[
I_{u2D}^2 = 100 \sqrt{\frac{\overline{u_u^2} + \overline{v_u^2}}{\overline{u_u^2} + \overline{v_u^2}}} \]

Fig. 2. Schematic side view of the experimental setup. The origin \(O(0,0,0)\) is chosen at the rotor centre.

Fig. 1. IFREMER’s Boulogne-sur-Mer flume tank description.
Similarly, this 2D quantity can be computed in the xOz plane as well, but it is irrelevant for the results presented hereafter.

In the present study, two different ambient turbulence conditions are considered. The turbulence in the flume tank is induced by the current generation process. As a matter of fact, without the use of a honeycomb, the natural ambient turbulence intensity of the flow is about $I_{ax} = 15\%$. A smoother flow may be obtained by the use of honeycombs and the turbulence intensity then reduces to about $I_{ax} = 3\%$. In the sequel, those two turbulence conditions will simply be referred to as $I_{ax} = 15\%$ (without honeycombs) and $I_{ax} = 3\%$ (with honeycombs). These values were obtained by LDV measurements of $(u,v)$ and $(u,w)$ at different points in the area swept by the turbine blades.

Table 2 presents measured values of $I_{ax}$ and $I_{ax}^{2D}$ for different upstream flow conditions: the above mentioned turbulence intensity conditions $I_{ax} = 3\%$ (Table 2a) and $I_{ax} = 15\%$ (Table 2b), together with different upstream velocity conditions $U_{ax}$. Whatever the upstream velocity $U_{ax}$, for a given $I_{ax}$ condition, the measured values of $I_{ax}$ or $I_{ax}^{2D}$ remain close to each other. Moreover, the measured $I_{ax}$ is always close to the indicative $I_{ax}$ value (3\% or 15\%). However, it should be stressed that the corresponding 2D turbulence intensity $I_{ax}^{2D}$ slightly differs from the indicative values of 3\% or 15\%. In particular, with $I_{ax} = 15\%$, the $I_{ax}^{2D}$ values are significantly below their 3D counterparts, more precisely $I_{ax}^{2D} < 13\%$. This is due to the omission of the $z$-components $W_{ax}$ and $\sigma(W_{ax})$ in the 2D evaluation, whose influence is non-negligible in the $I_{ax} = 15\%$ turbulence condition. This remark justifies the use of $I_{ax}^{2D}$ as a comparison basis when studying the wake in terms of downstream turbulence intensity (cf. Section 4), which is measured in 2D (cf. Section 2.7).

The mean upstream axial velocity $\bar{U}_{ax}$ may be simply denoted by $U_{ax}$. Five upstream velocities (from $U_{ax} = 0.4$ to 1.2 m s$^{-1}$) are considered with $I_{ax} = 3\%$, while four velocities (from $U_{ax} = 0.41$ to 1.03 m s$^{-1}$) are considered with $I_{ax} = 15\%$. Fig. 3 gives the profiles of the $u_{ax}$ and $v_{ax}$ upstream velocity components across the tank, in terms of mean value and standard deviation, for both considered turbulence intensity ranges and $U_{ax} = 0.8$ m s$^{-1}$.

2.4. Turbine model description

The model consists of a three-bladed horizontal axis turbine, which is $D = 2R = 0.7$ m in diameter. The rotor is connected to a motor-gearbox assembly consisting of a gearbox, a DC motor, a ballast load and a motor speed control unit [25], providing an active motor-gearbox assembly consisting of a gearbox, a DC motor, a ballast load and a motor speed control. The turbine blades are designed from a NACA 63418 profile. A more detailed profile description is given in Table 3.

The blockage ratio $\alpha$ is defined as the ratio between the rotor cross-section area $S = \pi R^2$ and the flume tank transverse area $A = W \cdot H$:

$$\alpha = \frac{S}{A} = \frac{\pi R^2}{W \cdot H}$$  

(8)

Table 2

<table>
<thead>
<tr>
<th>$U_{ax}$ [m s$^{-1}$]</th>
<th>$I_{ax}$ [%]</th>
<th>$I_{ax}^{2D}$ [%]</th>
<th>$U_{ax}$ [m s$^{-1}$]</th>
<th>$I_{ax}$ [%]</th>
<th>$I_{ax}^{2D}$ [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.4</td>
<td>2.7</td>
<td>3.2</td>
<td>0.4</td>
<td>15.3</td>
<td>14.6</td>
</tr>
<tr>
<td>0.6</td>
<td>2.6</td>
<td>3.1</td>
<td>0.6</td>
<td>14.7</td>
<td>13.0</td>
</tr>
<tr>
<td>0.8</td>
<td>2.7</td>
<td>3.1</td>
<td>0.8</td>
<td>14.7</td>
<td>13.3</td>
</tr>
<tr>
<td>1.0</td>
<td>2.7</td>
<td>3.1</td>
<td>1.0</td>
<td>14.7</td>
<td>14.0</td>
</tr>
<tr>
<td>(a) $I_{ax} = 3%$</td>
<td>(b) $I_{ax} = 15%$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

where $W = 4$ m and $H = 2$ m respectively denote the flume tank width and depth. In our study, the blockage ratio is then around $\alpha \approx 4.8\%$.

The Tip Speed Ratio (TSR) is classically defined as the ratio between the tip velocity and the upstream flow velocity as follows:

$$TSR = \frac{\Omega R}{U_{ax}} = \frac{\Omega_{aw} R}{U_{ax}}.$$  

(9)

where $\Omega$ is the rotor angular velocity and $\Omega_{aw}$ is thus the axial rotation speed, $R$ is the rotor radius and $U_{ax}$ is the upstream flow velocity. In our study, the turbine TSR varies from 0 to 10.

Finally, the radius-based Reynolds number is given by:

$$Re_x = \frac{U_{ax} R}{r}$$  

(10)

where $r$ denotes the fluid kinematic viscosity and is approximately $r \approx 10^{-6}$ m$^2$ s$^{-1}$. The studied Reynolds number range is then directly deduced from the $U_{ax}$ range mentioned above, which gives $Re_x \in [140,000;420,000]$. The whole structure description summary is presented in Table 4a and a picture is given in Fig. 4b.

2.5. Force and moment measurements

The force acting on the structure is obtained by means of a six-components load cell, which measures the three force components and the three moment components, at a 100 Hz acquisition frequency. A torque sensor, directly fixed between the rotor and the motor, provides a more accurate measurement of the axial torque than the one given by the load cell, at a 100 Hz acquisition frequency as well.

The power coefficient $C_P$ is defined as the proportion of power $P$ retrieved by the turbine as compared to the maximum available power $P_{ax}$ from the incoming flow through the rotor area $S$:

$$C_P = \frac{P}{P_{ax}} = \frac{\mu_b \Omega_{ax}}{\frac{1}{2} \mu_b S U_{ax}^3} = \frac{\mu_b \Omega_{ax}}{\frac{1}{2} \rho \pi R^2 U_{ax}^3}.$$  

(11)

where $\mu$ is the fluid density, $S = \pi R^2$ is the turbine cross-section area and $\mu_b$ is the axial moment -- or torque, defined as the x-component moment. Similarly, the thrust coefficient $C_T$ is defined as the axial force $F_x$ acting upon the turbine as compared to the kinetic energy of the incoming flow through $S$:

$$C_T = \frac{F_x}{\frac{1}{2} \rho \pi R^3 U_{ax}^2}.$$  

(12)

The $F_x$ measured here actually includes the axial force on the whole structure, that is the blades, the hub and the mast. Obviously, the $C_P$ and $C_T$ values used to compute those coefficients are time-averaged values. The measurement (and thus the averaging) duration is $T = 100$ s, which provides converged values of $C_P$ and $C_T$ (cf. Appendix C).

2.6. LDV measurements

The flow velocity measurements are performed by means of a Laser Doppler Velocimetry (LDV) system described in Refs. [21,26]. The LDV measurements are performed on a grid whose nodes $(X_i,Y_j)$ are arranged as follows:

- $X_i = 1.2D$ and $X_i = i \times D$ for $i = 2,\ldots,10$;
- $Y_i = -1.2 + (i-1) \times 0.1$ m for $i = 1,\ldots,25$, with two additional positions $Y_{26} = -Y_{27} = R = 0.35$ m.
The laser used for the measurements is described in Table 4. The discrete time-averaged velocity, corresponding to the mean value $u_N$ (resp. $v_N$), while error bars represent the corresponding standard deviations ($u_N$) (resp. $v_N$).

Figure 3. Upstream $u_*$ and $v_*$ velocity profiles across the tank, for $I_\infty = 3\%$ with $U_\infty = 0.8$ m s$^{-1}$ (left), and $I_\infty = 15\%$ with $U_\infty = 0.83$ m s$^{-1}$ (right). Symbols $\Box$ (resp. $\circ$) represent the mean value $\Pi_*$ (resp. $\Pi_*$), while error bars represent the corresponding standard deviation $\sigma(u_*)$ (resp. $\sigma(v_*)$).

2.8. Integrated velocity and turbulence intensity on a disc

A commonly used way of evaluating the velocity deficit is to consider the centreline velocity deficit, that is to say the velocity deficit at punctual locations along the turbine axis, defined at a given distance $x$ from the turbine as follows:

$$\gamma(x) = \left(1 - \frac{u(x,0,0)}{U_\infty}\right).$$

And thus, the centreline axial velocity deficit at given location $(x,0,0)$, expressed as a percentage, is naturally defined as:

$$\gamma_0(x) = 100\left(1 - \frac{\Pi_0(x)}{U_\infty}\right).$$

It is important to note that in the case of radial gradient in the velocity profiles, the centreline velocity deficit may not be a relevant indicator of the actual velocity deficit in the whole turbine’s area of influence. In order to further evaluate the velocity deficit as it would be perceived by a potential downstream turbine, a velocity deficit integrated on a disc is defined at a point $O_x(x,0,0)$ located at a given distance $x$ from the upstream turbine. The disc is parallel to the cross-sectional area of the turbine, that is to say it is defined in the $yO_z$ plane. Figure 5a depicts such a disc at some arbitrary location $O_x$ with some arbitrary radius $r$, whose choice will be discussed later on. The disc-integrated velocity (from which is computed the disc-integrated deficit) is then obtained by computing the integral in an ad hoc polar coordinate system.

In the case of axi-symmetric velocity profiles, the disc integral would reduce to a one-dimensional integral depending on the radial coordinate only. This radial coordinate is naturally set to be $|y|$. However, as the velocity profile is not exactly axi-symmetric [21,22], the final integrated value is obtained by taking the mean of those two integrals. The integration is performed successively for positive and negative values of $y$, that is to say on $[0;r]$ and $[-r;0]$. This integration process is illustrated on Fig. 5b.

Finally, the resulting disc-integrated mean velocity is normalised by the disc-integrated value of $U_\infty$ in order to make it dimension-free. Thus, the mean axial velocity at a given location $O_x(x,0,0)$, integrated on a disc $D(O_x,r)$ of centre $O_x$ and radius $r$ defined in the $yO_z$ plane is eventually given by:

$$\tilde{\Pi}_r(x) = \frac{\int\int_{D(O_x,r)} \Pi(x,y,z) \, dydz}{\int\int_{D(O_x,r)} U_\infty \, dydz} = \frac{\int\int_{D(O_x,r)} \Pi(x,y,z) \, dydz}{U_\infty \int\int_{D(O_x,r)} \, dydz} = \frac{\Pi_r(x)}{U_\infty}.$$
\[ \dot{\gamma}_t(x) = 100 \left( \frac{U_w - \bar{U}_r(x)}{U_w} \right) = 100 \left( 1 - \frac{\bar{U}_r(x)}{U_w} \right), \] (22)

The same disc-integration process can be carried out on the turbulence intensity. The mean turbulence intensity rate at given location \( O_z(x,0,0) \), integrated on \( D(O_z; r) \), is then given by:

\[ \bar{I}_r(x) = \frac{1}{r^2} \int_{D(O_z; r)} \int_{D(O_z; r)} |I(x,y,z)| dy dz, \] (23)

while the commonly used centreline turbulence intensity rate at given location \( O_z(x,0,0) \) is basically given by:

\[ I_0(x) = I(x,0,0). \] (24)

2.9. Dimension-free quantities

Every presented quantity is made dimension-free by dividing it by a characteristic homogeneous quantity. Most of these dimension-free quantities have just been presented in this section. Besides, any length is made dimension-free by means of the rotor diameter \( D \), and any flow velocity is made dimension-free by means of the upstream axial velocity \( U_w \).

Moreover, the dimension-free version of any dimensional quantity \( q \) is denoted by \( q' \). However, some quantities are directly presented dimension-free, because they do not have any dimensional version or because their dimensional version is irrelevant. This is the case, for example, of \( I, \gamma_{0r} \). Other specific dimension-free quantities such as the Tip Speed Ratio (TSR) or the thrust and power coefficients (\( C_T \) and \( C_p \)) are, of course, denoted as in the literature. Table 5 is a summary of the dimension-free quantities and their corresponding dimensional versions.

3. Performance evaluation

Several studies have been carried out on the evaluation of marine current turbines performances [13,21]. The present study really aims at giving complete and detailed data sets of both turbine performances (i.e. power and thrust coefficients) and wake flow characterisation (Section 4). A previous study [21] was presented in a similar manner but the turbine blade profiles were confidential. As a consequence, all the results were made dimension-free by some unknown coefficient, which makes comparisons with new studies impossible. Another significant difference stems in the torque measurement, which is now performed with a torque sensor rather than the load cell, so as to obtain more accurate and less

![Fig. 4. Turbine model description.](image-url)
noisy measurements (see Appendix C). The main goal here is to provide the scientific community with relevant data sets for comparison with future studies. Additionally, \( C_P \) and \( C_T \) representative spectra are shown in Appendix D. More detailed spectral analyses were carried out on similar configurations by Maganga et al. [21] and Gaurier et al. [27].

3.1. Power coefficient

Fig. 6a and b depict the performance curves for different upstream velocities \( U_{\infty} \) and the two studied ambient turbulence intensities, namely \( I_{\infty} = 3\% \) and \( I_{\infty} = 15\% \). Except for \( U_{\infty} = 0.4 \text{ m s}^{-1} \) with the lower ambient turbulence intensity, the turbine operates properly and the \( C_P \) curves are very similar to those presented in the literature [13,21]. For both ambient turbulence intensities, it is striking to observe that the turbine operating range is always contained in \( 3 \leq \text{TSR} \leq 6 \). For \( I_{\infty} = 3\% \) and except for \( U_{\infty} = 0.4 \text{ m s}^{-1} \), the \( C_P \) values are always slightly above 0.4 (Fig. 6a), whereas they are slightly below this value for almost every upstream velocity at \( I_{\infty} = 15\% \) (Fig. 6b). However, except for \( U_{\infty} = 0.4 \text{ m s}^{-1} \) again, the \( C_P \) curves tend to collapse into a single curve for \( I_{\infty} = 3\% \) all over the TSR range, while they tend to differ for \( I_{\infty} = 15\% \). With this ambient turbulence intensity, the higher the upstream velocity \( U_{\infty} \), the higher the \( C_P \) curve. Indeed, the maximum \( C_P \) for \( U_{\infty} = 0.83 \) or 0.62 \text{ m s}^{-1} is almost 10\% lower than for \( U_{\infty} = 1.03 \text{ m s}^{-1} \). In addition, difference between the curves increase with the TSR.

3.2. Thrust coefficient

The thrust evolution of the considered turbine also leads to a similar conclusion: the turbine behaviour is weakly dependent on the ambient turbulent intensity \( I_{\infty} \). In fact, all the \( C_T \) curves almost superimpose for \( I_{\infty} = 3\% \) (Fig. 7a), except once more for \( U_{\infty} = 0.4 \text{ m s}^{-1} \), as for the \( C_P \) curves. In the operating range \( 3 \leq \text{TSR} \leq 6 \), the \( C_T \) values increase from approximately 0.7 to plateau of about 0.80 or 0.85 from \( \text{TSR} = 4 \) even until the last TSR value (\( \text{TSR} \approx 8 \)). A similar analysis can be performed for \( I_{\infty} = 15\% \) (Fig. 7b), the two main differences being that the \( C_T \) curves all superimpose without exception (except for \( U_{\infty} = 0.41 \text{ m s}^{-1} \) to 1.03 \text{ m s}^{-1} and that there is no distinct plateau. In the operating range, the curves increase from \( C_T = 0.7 \) to a maximum value of 0.8 approximately at \( \text{TSR} = 6 \), and then decreases.

3.3. Standard deviation

Nevertheless, the ambient turbulence intensity \( I_{\infty} \) does have a significant influence, not on the mean values of \( C_P \) and \( C_T \), but on their standard deviation values (\( \sigma_{C_P} \) and \( \sigma_{C_T} \), depicted on Fig. 8a and b. Indeed, whatever the \( C_P \) or \( C_T \) in the operating range, \( \sigma_{C_P} \) and \( \sigma_{C_T} \) are always somehow 2.5 times higher with \( I_{\infty} = 15\% \) than with \( I_{\infty} = 3\% \). The observation is still valid outside the operating range in the upper part of the TSR values (i.e. \( \text{TSR} \geq 6 \)). However, for lower values (i.e. \( \text{TSR} \leq 3 \)), \( \sigma_{C_P} \) tends to collapse into a single curve whatever the ambient turbulence intensity \( I_{\infty} \), whereas \( \sigma_{C_T} \) remains almost twice higher with \( I_{\infty} = 15\% \). The described behaviour is valid whatever the upstream velocity value except for \( U_{\infty} = 0.4 \text{ m s}^{-1} \) with \( I_{\infty} = 3\% \) as discussed earlier. The fact that \( \sigma_{C_P} \) and \( \sigma_{C_T} \) are always 2.5 times higher with \( I_{\infty} = 15\% \) than with \( I_{\infty} = 3\% \) is far from being negligible.

3.4. Discussion

In terms of industrial applications, the relatively similar power and thrust behaviour of the studied turbine is an interesting feature because it enables its installation whatever the environmental ambient turbulence. This observation is also appropriate if the turbulence intensity varies with time at a precise location, either through the action of the tide or owing to the weather conditions. This turbine geometry (blade profile, length, chord and twist) makes it very robust to ambient upstream velocity conditions, which represents an important issue in the event of interaction...
effects between turbines. As a matter of fact, in a turbine wake, the turbulence intensity increases. However, medium to small scales coherent structures appear and add to the initially homogeneous turbulence. Consequently, the downstream turbine does not recover its turbulence upstream conditions even after 10 diameters, where the velocity deficit remains well pronounced even 10 diameters downstream (cf. Fig. 9b).

As concerns the fatigue of blades [20,27], as well as gear boxes and electrical generators, standard deviation of both power and thrust coefficients may have a major impact especially on the design and hence, on the global cost of the machine.

The ambient turbulence intensity thus influences the machine behaviour, in terms of maximum retrieved power to a small extent, but most importantly and to a larger extent, in terms of force and torque fluctuations.

4. Wake characterisation

4.1. Velocity, turbulence intensity and Reynolds shear stress maps

Fig. 9 presents mean axial velocity, turbulence intensity rate and Reynolds shear stress maps, from 1.2D to 10D downstream of the turbine. The upstream velocity is 0.8 m s\(^{-1}\) and the turbine TSR is 3.67. As previously, two upstream turbulence intensity rates are considered and compared, namely \(I_u = 3\%\) and \(I_u = 15\%\). In order to make our experimental data available in a more convenient way, velocity and turbulence intensity profiles behind the turbine are provided in Appendix A.

The first striking observation is that the wake effects decrease much faster with a higher upstream turbulence level, in terms of both axial velocity deficit and downstream turbulence intensity rate. As a matter of fact, while with \(I_u = 3\%\), the velocity deficit remains well pronounced even 10 diameters downstream (cf. Fig. 9a), with \(I_u = 15\%\), the flow recovers most of its velocity from 6 diameters (cf. Fig. 9b).

The same observation holds for the downstream turbulence intensity rate. With \(I_u = 3\%\), the flow does not recover its turbulence upstream conditions even after 10 diameters, where the turbulence intensity rate remains much higher than 3\%, with approximately 9\%. It is striking to realise that the turbulence intensity peak is not located immediately behind the turbine, but

\[
\gamma_r(x) = 100 \left(1 - \frac{u(x,0)}{U_u} \right) \quad \text{Eq. (18)}
\]

\[
\gamma_h(x) = 100 \left(1 - \frac{u(x,0)}{U_u} \right) \quad \text{Eq. (22)}
\]

\[
I_u, I_v, I_u(x,y,z), I_v(x), I_v(x) \quad \text{Eqs. (6), (7), (15), (23), (24)}
\]

\[
\Pi = \sqrt{\frac{\partial u^2}{\bar{u}^2}} \quad \text{Eq. (16)}
\]

\[
\text{TSR} = \left(\frac{1}{U_R/U_w} \right) \quad \text{Eq. (9)}
\]

\[
C_T = -m x \Omega_1 \left(\frac{1}{2 \rho n R^2 U_w^3} \right) \quad \text{Eq. (11)}
\]

\[
C_I = -R \left(\frac{1}{2 \rho n R^2 U_w^3} \right) \quad \text{Eq. (12)}
\]
between 5 and 7 diameters downstream. This is consistent with previous observations made by Refs. [17,21], for instance. Looking at the velocity profiles (Fig. A.12 in Appendix A), one can observe that this high turbulence intensity zone exactly corresponds to a modification in the velocity profiles shape, from a top hat to a bell shape velocity profile. This kind of shape transition has already been identified in a previous study [21] with a different turbine configuration, in a flow with a turbulence intensity rate of 5%. This shape modification in the velocity profiles is linked to the merging of the mixing layers. On Fig. 9e, the merging of the two mixing layers can clearly be identified between \(x^* = 5\) and 7. On the contrary, with \(I_\infty = 15\%\), the highest turbulence intensity zone is observed in the near wake of the turbine (0 ≤ \(x^*\) ≤ 3) and rapidly decreases. In addition, the upstream conditions are fully recovered 10 diameters downstream.

Another observation that can be drawn from Fig. 9 is that the wake shape is larger and more diffuse with \(I_\infty = 15\%\) than it is with \(I_\infty = 3\%\). On the one hand, with \(I_\infty = 3\%\), both axial velocity and turbulence intensity are only disturbed in a limited axial strip, which is approximately one diameter large and axially aligned with the turbine. This strip slightly enlarges along with flow direction to become between 1.5 and 2 diameters large at 10 diameters downstream of the turbine. On the other hand, with \(I_\infty = 15\%\), the wake shape is less easily distinguishable. It rapidly spreads out in

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**Fig. 8.** Standard deviation of the power \(C_p\) (left) and thrust \(C_T\) (right) coefficients, for \(I_\infty = 3\%\) and 15%.

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**Fig. 9.** Wake behind a turbine with TSR = 3.67, \(U_\infty = 0.8\) m s\(^{-1}\) and for \(I_\infty = 3\%\) (left) and \(I_\infty = 15\%\) (right).
radial directions, unlike with $I_w = 3\%$. These last observations are clearly related to the Reynolds shear stress maps depicted on Fig. 9e and f. From Fig. 9e ($I_w = 3\%$), two zones can easily be distinguished. For $0 \leq x' \leq 5$, the shear layers start very thin just behind the turbine and grow thicker. Indeed, from $x' \geq 5$, the shear layers are much larger. The first zone ($0 \leq x' \leq 5$) corresponds to sharp velocity gradients (cf. Fig. 10 and Fig. A12a in Appendix A). The presence of blade tip vortices was also observed for a similar configuration [21].

Since the upstream flow has a low ambient turbulence intensity rate, $I_w = 3\%$, the shear layers naturally develop without being too much perturbed by the upstream turbulence. For $x' \geq 5$, the shear layers have completely developed and start to merge. This merging zone $5 \leq x' \leq 7$ clearly corresponds to the highest turbulence intensity zone observed on Fig. 9c. This last observation is another characteristic of the transition from a top hat to a bell shape velocity profile. Despite the differences in the turbulence configuration (especially the blade design), its rotation speed and the ambient turbulence intensity, the wake behaviour with $I_w = 3\%$ is very similar to the one described in Ref. [21] with $I_w = 5\%$.

However, comparing the Reynolds shear stress values between Fig. 9e and f clearly indicates that the flow morphology is somehow different with a higher turbulence intensity. The Reynolds shear stress maximum value is about 1.5 times higher with $I_w = 15\%$ than with $I_w = 3\%$, all other parameters equal. This indicates that the mixing is much more efficient with $I_w = 15\%$ than it is with the lower value.

As a matter of partial conclusion, the influence of ambient turbulence turns out to be significant. The higher the ambient turbulence intensity, the better the mixing and consequently, the shorter and weaker the wake influence.

4.2. Disc-integrated velocity defect and turbulence intensity

Fig. 10 illustrates the differences between the different evaluations of the velocity deficit in the near wake of a turbine (cf. Section 2.8). For the disc-integrated velocity (Eq. (21)), two values of $r$ are chosen. The first natural value is $R$, the turbine rotor radius. The second, $R^+$, slightly enlarges the integration area to the further two measured points along $y$. In other words, it enlarges the presumed wake area that would be perceived by a potential downstream turbine. Furthermore, together with $\overline{D_p}(x)$, those three values are useful to evaluate how homogeneous the flow is in this area.

Indeed, if $\overline{D_p}(x)$ and $\overline{\Delta_p}(x)$ are similar, this means that the flow velocity is almost homogeneous on $D(O_z, R)$. Conversely, if these values significantly differ, this indicates that high radial gradients are present in this area. The same remark holds for the difference between $\overline{\Delta_p}(x)$ and $\overline{\Delta_p}(x)$, except it indicates how homogeneous the flow is in the ring $D(O_z, R^+) - D(O_z, R)$.

The axial velocity profile depicted in Fig. 10 is the first profile (issuing from Fig. 9a) measured in the wake of a turbine immersed in an incoming flow with a low turbulence intensity rate $I_w = 3\%$. The velocity profile $\overline{\Delta_p}(y')$ clearly has a top hat shape. As discussed in Section 2.8, the velocity profile is not axi-symmetric. More precisely, the perturbation observed between $-0.5 \leq y' \leq 0$ can be attributed to the interaction between the wake and the maintaining mast (see photography in Fig. 4b or Fig. 2). This asymmetry has also been observed for wind turbines [28]. In addition, the values of $\overline{D_p}(x)$, $\overline{\Delta_p}(x)$ and $\overline{\Delta_p}(x)$ are rather different, as it was expected. If one wants to evaluate the power that would perceive a turbine situated in the wake, using the value of $\overline{D_p}(x)$ would clearly underestimate the potential power. Using the values $\overline{\Delta_p}(x)$ or $\overline{\Delta_p}(x)$ would improve the estimation but, owing to the sharp gradients at the shear layer location ($0.4 < \vert y' \vert < 0.6$), the difference between those two values is not negligible. The use of these three indicators of velocity would be of great interest, especially in the case of interactions that are discussed in Part II [1] of the present study. The difference between the centreline and the integrated deficits illustrates the heterogeneity of the flow at a given location.

Fig. 11 translates Fig. 9a–d in terms of centreline and disc-integrated velocity deficit (Eqs. (18) and (22)) and turbulence intensity rate (Eqs. (23) and (24)). A comparison of Fig. 11a and b provides valuable information. First, the three values of $\gamma_0$, $\gamma_R$ or $\gamma_R$ never converge for an ambient turbulence intensity of $3\%$. This behaviour was expected as the wake is well characterised even at 10 diameters behind the turbine. On the contrary, for $I_w = 15\%$, $\gamma_0$, $\gamma_R$ and $\gamma_R$ remain rather different only until $x' = 3$ corresponding to the highest Reynolds shear stress area in Fig. 9f. Then, $\gamma_R$ and $\gamma_R$ almost superimpose from $x' = 3$, whereas $\gamma_0$ still differs. Finally, the three indicators are very similar for $x' \geq 5$, where the wake flow is hardly visible, which corresponds to the end of the wake (cf. Fig. 9b and d). As a matter of conclusion, these indicators provide precise information about the wake shape.

Another piece of information from these graphs is that the mean velocity deficit remains around 20% even 10 diameters behind the turbine for $I_w = 3\%$. This 20% velocity deficit at 10 diameters ($\overline{\Delta_p}(10D) \approx 0.8U_w$) actually corresponds to approximately 50% of available power deficit at this location ($\overline{P}(10D) \approx 0.5P_{\max}$). Indeed, as mentioned for the definition of the power coefficient (11), the maximum available power is proportional to the velocity cubed, all other parameters (fluid density, rotor radius) being constant.

A 20% mean velocity deficit is however obtained at $x' \approx 3$ for $I_w = 15\%$, then decreasing to approximately 10% at $x' \approx 5$ and finally to less than 5% 10 diameters downstream. As a matter of comparison, the power deficit for $I_w = 15\%$ is approximately 15% at 10 diameters compared to the 50% for $I_w = 3\%$ at the same location. These observations are very important, especially regarding the fact that the turbine performances, in terms of power coefficient $C_p$ are only little influenced by the ambient turbulence (Fig. 6a and b). This point is a crucial issue in terms of implanting a turbine in an array, which will be treated in Part II [1].

Regarding the turbulence in the turbine wakes for the two studied ambient turbulence intensity rates, Fig. 11c and d also illustrate most of the characterising features of the wake flow. First, for $I_w = 3\%$, in the whole wake ($0 \leq x' \leq 10$ for this study), the three indicators $I_0$, $I_R$ or $I_R$ are all contained between 10% and 22%. The minimum value is however 3 to 4 times higher than the ambient level of $I_w = 3.1\%$, corresponding to $I_w = 3\%$. From Fig. 11c one can
also clearly identify the three main characteristics of the flow field. For $x^*/C_{20} \geq 3$, $I_0$ is very high with 22% corresponding to the hub wake (cf. Fig. A.13a in Appendix A), precisely located at the wake centre and decaying through diffusion. On the contrary, $I_R$ or $I_{k_2}$ are rather low owing to the fact that, except for the centreline and the thin vortical shear layer issuing from the blade tips, the turbulence intensity is also very low. The merging zone identified earlier (see Section 4.1) can also be distinguished between $4 \leq x^* \leq 7$, characterised by a peak in $I_2$ or $I_{k_2}$ as well. Those last two indicators increase from $x^* \approx 0$ owing to the expansion of the shear layers, until their merging at this location, resulting in these higher values. Finally, from $x^* \geq 7$, the three indicators become rather similar with $I_0$ slightly higher due to a bell shape wake.

Concerning the three indicators for $L_\infty = 15\%$, the situation is completely different. As already observed on Fig. 9f, the merging of the shear layer appears early in the wake flow, just after the blades and until $x^* \approx 3$. This merging zone is characterised, as for $L_\infty = 3\%$, by a higher value of $I_2$ ($I_0 \approx 32\%$ at $x^* = 1.2$) and similar lower values of $I_R$ and $I_{k_2}$. From $x^* \geq 3$, the bell shape profiles are clearly identifiable (cf. Appendix A) and this phenomenon is characterised by the fact that, from $x^* \approx 5$, the three indicators tend to collapse into a single curve which is obvious for $x^* \geq 7$. In addition, from $x^* \geq 7$, $I_0$, $I_R$ or $I_{k_2}$ are identical and equal to the ambient initial value of $I_{0w} = 13.3\%$ corresponding to $L_\infty = 15\%$.

As a matter of conclusion for $L_\infty = 15\%$, from Fig. 11b and d, one can see that for the studied turbine in the studied conditions, after $x^* = 6$ or 7, the flow conditions are almost identical to the ambient upstream condition with only 5\% velocity deficit and the recovered ambient turbulence intensity. At this location of the flow, no more coherent flow patterns can be found and, in the case of a potential second turbine downstream, this turbine would apparently experience ambient inflow conditions with a power deficit of only 15\% corresponding to a 5\% velocity deficit. The above described situation will be tested and assessed in Part II [1] of the present study.

5. Conclusions and prospects

This study has pointed out the significant role of the ambient turbulence intensity rate on the behaviour of a 3-bladed horizontal axis marine current turbine. First of all, for this precise turbine, the mean performances are hardly influenced by this parameter, which makes it possible to implant turbines with the same design in sites with different turbulence intensity conditions, without too much loss of overall efficiency. In addition, the mean turbine performances should remain stable in time, even if variations of the ambient turbulence conditions occur. However, the performance fluctuations dramatically increase with the turbulence intensity. This may have a major impact on the fatigue of the machine, and thus on its global manufacturing cost [20,27].

The ambient turbulence intensity also has a considerable influence on the turbine wake. As a matter of fact, the wake shape, length and strength largely depend on the upstream turbulence conditions. On the one hand, with $L_\infty = 3\%$, the wake remains pronounced even ten diameters downstream of the turbine, with almost 20\% velocity deficit and more than three times the upstream ambient turbulence intensity. Furthermore, the shear layers are still visible, which expresses the presence of coherent vortical structures, and thus the flow homogeneity is still not recovered. On the other hand, with a higher turbulence intensity, $L_\infty = 15\%$, the wake dissipates much faster. Indeed, the upstream conditions, in terms of velocity, turbulence intensity and shear stress, are almost fully
recovered six diameters downstream, where the flow becomes homogeneous again.

Further studies should now be carried out on the wake characterisation behind a turbine with a lower TSR (e.g., TSR ≈ 3, for which the loss of power is only about 15%) in a $I_B = 3\%$ turbulence condition. The wake may then be less pronounced, which could allow a closer second turbine implantation.

As a conclusion, in the context of farm implantation, a second turbine, located at a given distance in the direct wake of the upstream turbine, should recover more energy if the upstream flow has a high turbulence intensity. This high turbulence advantage is counterbalanced by the fact that such conditions also imply more force fluctuation and thus accelerate the machine wear. The issue of interactions between two aligned marine current turbines was also investigated and will be discussed in the second part of this paper [1].

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### Appendix A. Wake profiles

Fig. A.12 presents axial velocity profiles at several distances downstream of the turbine, for both $I_B = 3\%$ (Fig. A.12a) and $I_B = 15\%$ (Fig. A.12b).

Fig. A.13 presents downstream turbulence intensity profiles at several distances downstream of the turbine, for both $I_B = 3\%$ (Fig. A.13a) and $I_B = 15\%$ (Fig. A.13b).

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**Fig. A.12.** Axial velocity profiles with TSR = 3.67, $U_B = 0.8$ m s$^{-1}$ and for $I_B = 3\%$ (top) and $I_B = 15\%$ (bottom).
Appendix B. Convergence results for LDV measurements

In order to justify the use of 100 seconds as a LDV measurement duration, convergence graphs are presented at nine different strategic points downstream of the turbine. Fig. B.14 describes their location in the wake.

The TSR and the flow velocity $U_N$ are those of the previously presented experiments, that is to say $TSR = 3.67$ and $U_N = 0.8$ m s$^{-1}$ (for $I_N = 3\%$) or $U_N = 0.83$ m s$^{-1}$ (for $I_N = 15\%$). Several measured quantities are shown, namely the axial velocity $u$, the radial velocity $v$, the Reynolds first and second normal stresses $s_{2u}$ and $s_{2v}$, the Reynolds shear stress $\overline{uv}$ and the turbulence intensity rate $I$.

Fig. B.15 presents the convergence results with $I_N = 3\%$. Time-averaged quantities $\overline{q}$ are plotted against the averaging duration $t$. The graphs show that the average seems to be converged very early, around $t = 50$ s. Therefore, $T = 100$ s is a correct measurement (and thus averaging) duration.

Likewise, Fig. B.16 presents the convergence results with $I_N = 15\%$. The convergence seems to appear a little later, around $t = 80$ s. $T = 100$ s is then still an appropriate measurement duration.

Fig. A.13. Downstream turbulence intensity profiles with $I_N = 3\%$ (top) and $I_N = 15\%$ (bottom).
Fig. B.14. LDV measurement points for convergence checking.

Fig. B.15. Convergence of various time-averaged quantities as a function of the measurement time $t$, with $\text{TSR} = 3.67$, $U_N = 0.8 \text{ m s}^{-1}$ and $I_N = 3\%$.

(a) Axial velocity $\bar{u}$
(b) Radial velocity $\bar{v}$
(c) Reynolds first normal stress $\bar{u'}u'' = \sigma_u$
(d) Reynolds second normal stress $\bar{v'}v'' = \sigma_v$
(e) Reynolds shear stress $\bar{u'}v''$
(f) Turbulence intensity rate $I$

Fig. B.15. Convergence of various time-averaged quantities as a function of the measurement time $t$, with $\text{TSR} = 3.67$, $U_N = 0.8 \text{ m s}^{-1}$ and $I_N = 3\%$. 
Appendix C. Convergence results for force and moment measurements

A convergence analysis on the force and moment measurements is also presented with $I_N = 15\%$. Time-averaged $C_T$ function of the averaging duration are shown on Figs. C.17 and C.18 for different $U_N$ and TSR conditions. Likewise, Figs. C.19 and C.20 present time-averaged $C_p$. For both quantities, the convergence seems to be reached from $t = 50 \text{ s}$. Again, $T = 100 \text{ s}$ is thus an appropriate measurement (and thus averaging) duration.

Fig. B.16. Convergence of various time-averaged quantities as a function of the measurement time $t$, with TSR $= 3.67$, $U_N = 0.83 \text{ m s}^{-1}$ and $I_N = 15\%$. 

Appendix C. Convergence results for force and moment measurements

A convergence analysis on the force and moment measurements is also presented with $I_N = 15\%$. Time-averaged $C_T$ function of the averaging duration are shown on Figs. C.17 and C.18 for different $U_N$ and TSR conditions. Likewise, Figs. C.19 and C.20 present time-averaged $C_p$. For both quantities, the convergence seems to be reached from $t = 50 \text{ s}$. Again, $T = 100 \text{ s}$ is thus an appropriate measurement (and thus averaging) duration.

Fig. B.16. Convergence of various time-averaged quantities as a function of the measurement time $t$, with TSR $= 3.67$, $U_N = 0.83 \text{ m s}^{-1}$ and $I_N = 15\%$. 

Appendix C. Convergence results for force and moment measurements

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Fig. B.16. Convergence of various time-averaged quantities as a function of the measurement time $t$, with TSR $= 3.67$, $U_N = 0.83 \text{ m s}^{-1}$ and $I_N = 15\%$. 

Appendix C. Convergence results for force and moment measurements

A convergence analysis on the force and moment measurements is also presented with $I_N = 15\%$. Time-averaged $C_T$ function of the averaging duration are shown on Figs. C.17 and C.18 for different $U_N$ and TSR conditions. Likewise, Figs. C.19 and C.20 present time-averaged $C_p$. For both quantities, the convergence seems to be reached from $t = 50 \text{ s}$. Again, $T = 100 \text{ s}$ is thus an appropriate measurement (and thus averaging) duration.

Fig. B.16. Convergence of various time-averaged quantities as a function of the measurement time $t$, with TSR $= 3.67$, $U_N = 0.83 \text{ m s}^{-1}$ and $I_N = 15\%$. 

Appendix C. Convergence results for force and moment measurements

A convergence analysis on the force and moment measurements is also presented with $I_N = 15\%$. Time-averaged $C_T$ function of the averaging duration are shown on Figs. C.17 and C.18 for different $U_N$ and TSR conditions. Likewise, Figs. C.19 and C.20 present time-averaged $C_p$. For both quantities, the convergence seems to be reached from $t = 50 \text{ s}$. Again, $T = 100 \text{ s}$ is thus an appropriate measurement (and thus averaging) duration.
Fig. C.17: Time-averaged $C_T$ convergence as a function of the measurement time $t$ for two given velocities $U_\infty = 0.41 \text{ m s}^{-1}$ (left) and $U_\infty = 0.83 \text{ m s}^{-1}$ (right), with $I_N = 15\%$. Three different TSR values are considered.

Fig. C.18: Time-averaged $C_T$ convergence as a function of the measurement time $t$ for two given TSR, TSR = 2.9 (left) and TSR = 5.8 (right), with $I_N = 15\%$ and various upstream velocities.

Fig. C.19: Time-averaged $C_T$ convergence as a function of the measurement time $t$ for two given velocities $U_\infty = 0.41 \text{ m s}^{-1}$ (left) and $U_\infty = 0.83 \text{ m s}^{-1}$ (right), with $I_N = 15\%$. Three different TSR values are considered.
Appendix D. Spectral analysis

Fig. D.21 shows the frequency spectra of the $C_T$ and $C_P$ measurements on the turbine $\text{TSR} = 2$ and for two upstream flow conditions. With $I_\infty = 3\%$ (Fig. D.21a), the $C_T$ spectrum clearly enables to identify the frequency of a blade passing before the mast $f_b$, owing to the induced modification of the axial force on the mast. The corresponding $C_P$ spectrum enables to identify the rotation frequency $f_r$, probably the blades slight imbalance. One can observe that $f_b \approx 2.23 \text{ Hz}$ consistently equals three times the rotation frequency $f_r \approx 0.74 \text{ Hz}$. The rotation velocity $|\Omega| = 2\pi f_r$ and thus the TSR can then be deduced thanks to Eq. (9). Here, the deduced TSR is 2.03 which is close to the nominative (prescribed) value of $\text{TSR} = 2$.

On the other hand, with $I_\infty = 15\%$, there is two much noise on both $C_P$ and $C_T$ signals and no frequency can be easily distinguished. It should be noted that similar and more detailed spectral analyses were carried out by Maganga et al. [21] and Gaurier et al. [27].

Fig. D.22 shows axial velocity fluctuation spectra of the upstream and wake flow. For both turbulence intensity rates, the upstream spectra show that the fluctuations are mostly low frequencies, below 1Hz. The wake spectra are obtained from measurements at point $P_2$ of Fig. B.14, that is right behind the turbine ($x = 1.2D$), right opposite the blade tip ($y = R$) where tip vortices emission is likely to occur. The spectra are slightly altered by the presence of the turbines. In addition, the blade passing frequency $f_b = 4.13 \text{ Hz}$ can be clearly identified with $I_\infty = 3\%$, probably thanks to tip vortices. This frequency corresponds to a $\text{TSR}$ of 3.78, which is close to the nominative value of $\text{TSR} = 3.67$. 

Fig. C.20. : Time-averaged $C_P$ convergence as a function of the measurement time $t$ for two given $\text{TSR}$, $\text{TSR} = 2.9$ (left) and $\text{TSR} = 5.8$ (right), with $I_\infty = 15\%$ and various upstream velocities.
Fig. D.22. Axial velocity fluctuation spectra of the upstream (\(u'_\infty\)) and wake (\(u'_f\)) flow. The wake measurement is performed at point \(P_3\) of Fig. B.14, i.e. at \(x = 1.2D\) and \(y = R\). Two upstream conditions are considered, namely \(I_\infty = 3\%\) and \(U_\infty = 0.8\ m\ s^{-1}\) on the one hand, and \(I_\infty = 15\%\) and \(U_\infty = 0.83\ m\ s^{-1}\) on the other hand.

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